

Regular Grammars

CS712

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A grammar is regular if each production takes one of the following forms, where uppercase letters are nonterminals and w is a nonempty string of terminals:

$$N \rightarrow \lambda$$

$$N \rightarrow w$$

$$N \rightarrow T$$

$$N \rightarrow wT$$

i.e. only one nonterminal can appear on the right side of a production, and it must appear at the right end of the right side.

Theorem Regular grammars generate exactly the set of regular languages.

Proof by construction

1) regular grammar to NFA

2) NFA to regular grammar

Key idea nonterminals \leftrightarrow states

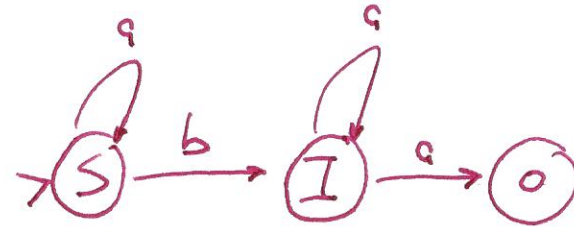
example regular grammar \rightarrow NFA

$$S \rightarrow a S$$

$$S \rightarrow b I$$

$$I \rightarrow a$$

$$I \rightarrow a I$$



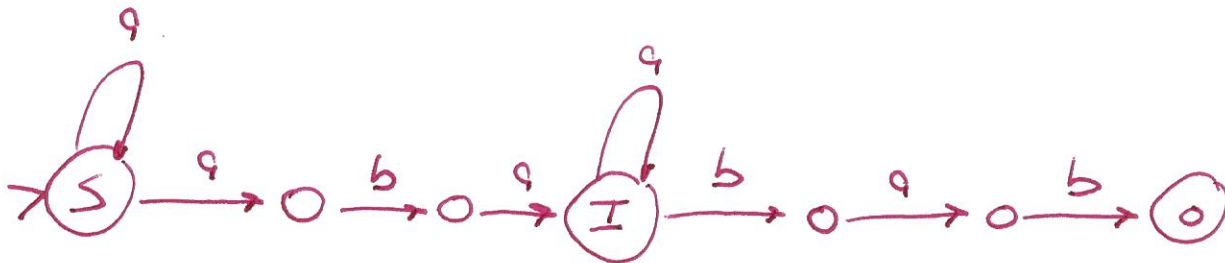
example regular grammar \rightarrow NFA

$$S \rightarrow a S$$

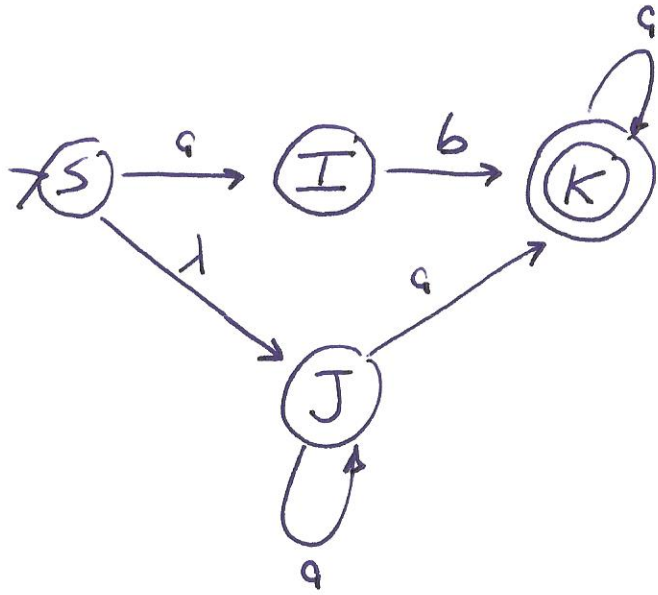
$$S \rightarrow a b a I$$

$$I \rightarrow b a b$$

$$I \rightarrow a I$$



example NFA \rightarrow regular grammar



$S \rightarrow a I$

$S \rightarrow J$

$I \rightarrow b K$

$J \rightarrow a J$

$J \rightarrow a K$

$K \rightarrow \lambda$

$K \rightarrow a K$

Key model final
state with
null rule

$S \rightarrow a I \rightarrow a b K \rightarrow a b a K \rightarrow a b a$